Cracking the Vigenère Cipher

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What is the Vigenère Cipher?

- Also known as the <u>Repeating Keyword</u> Cipher
- Polyalphabetic
 - More secure than monoalphabetic ciphers
 - Brute force algorithms can't decrypt it
 - Used more frequently than monoalphabetic ciphers

History

- Invented in 1553 by the Italian cryptographer Giovan Battista Bellaso
- Was known as "le chiffre indéchiffrable"
 - Means "the unbreakable cipher" or "the undecipherable cipher" in French
- Was known to be unbreakable for three centuries
- Broken by Charles Babbage

Example

- Example:
 - Plain Text: The Quick Brown Fox Jumps Over the Lazy Dog
 - Keyword: **Fox**
 - Cipher Text: Yvb Vifhy Ywcts Tlc Xrrdp Tjbw hej Zxem Atu

Assuming **a** is **0**

Plain - T = 19 Key - F = 5 Encrypted: (19 + 5) % 26 = 24 = Y

Plain – H = 7
Key – O = 14
Encrypted:
$$(7 + 14) \% 26 = 21 = V$$

- Step 1: Understanding ASCII
 - What is ASCII?
 - Represent: Numbers, Letters, Symbols with their respective Hex / Decimal / Binary representation.
 - Why is this necessary?
 - Very briefly:
 - $\mathbf{a} = 97, \, \mathbf{b} = 98, \, \dots, \, \mathbf{z} = 122$
 - Important with:
 - IO
 - In Python: 'a' = 97
 - Important! To Normalize this we do, 97 97 = 0 (First Letter in the Alphabet)
 - So, if we are pushing 'a' forward by 'c' spots, we don't accidentally shift it by 99.
 - **197 = ---** (Horizontal Bar) In Ascii

- Step 2: File IO
 - I will cover three brief points:
 - When Encrypting & Decrypting, file formatting is preserved.
 - Files are represented as **objects**
 - A simple Statement to check if a Character is Legal
 - return (ord(char) > 64 and ord(char) < 91) or (ord(char) > 96 and ord(char) < 123)
 - Ord() converts a Character to Decimal in **Python**
 - Checks to make sure the character is between **a-z**, **A-Z**

- Step 3: Methodology
 - Frequency Analysis.
 - Go through the file, gathering all letter frequencies.
 - First Checks for length 5, down to 1.
- Check out this excerpt:

LHVSY CEZZQ MPCWP UEVGH CWPWE FQHZZ WSYSV CEVGD SMUWN LHVSY HVSYC VSYCE

The program goes through **every** possible pair

(Yes, I stole this excerpt from Dr. Polhill's handout)

Example Cited

Ecwoqww, Ycsu. "Jcppy Doqqe pbo Rmjhdfo." Iwwe, 2022, qcwa.jwzdaf.llf/o2a/zp/jwyetbe/3258375/cqphRcyamye/27807694/Kwpd.

Keyword: Polhill

Polhill, John. "Break Shift and Keyword." Bolt, 2022, bolt.bloomu.edu/d2l/le/content/3258375/viewContent/27807694/View.

• Step 3: Continued

LHVSY CEZZQ MP**CWP** U**EVG**H **CWP**WE FQHZZ WSYSV C**EVG**D SMUWN GEZLG UFZCO PPGWF PHJOE HJSXO VVESC QSSTG LFGIY OYOCS QTHVC HJCWO CSFCT BIWEV KBVHJ SJAKU SHDSZ BVCZI TGNVG APDNS LGGPC WPUXS CPTUO ONHQC

- A **couple** repeated words are highlighted
- In my program, they are stored as so in a Dictionary:

{'CWP': {'InitPos': 12, 'Count': 3, 'Distance': 8}, 'EVG': {'InitPos': 16, 'Count': 2, 'Distance': 20} }

- Step 4: Finding Keyword Length
 - From the Previous Example:
 - Distance between CWP = 20
 - Distance between EVG = 8
 - GCD(20, 8) = 4
 - 4 is now a candidate for the length of the keyword.
 - The candidates get tallied as the program proceeds.
 - In <u>this</u> case the keyword length is indeed 4

- Step 5: Compare Cipher Text Frequencies to English Letter Frequencies
 - Since we decided on a length 4 keyword
 - $\cdot \;$ We can check every fourth letter

LHVS YCEZ ZQMP CWPU EVGH CWPW EFQH ZZWS YSVC EVGD SMUW NGEZ LGUF ZCOP PGWF PHJO EHJS XOVV ESCQ SSTG LFGI YOYO CSQT HVCH JCWO CSFC TBIW EVKB VHJS JAKU SHDS ZBVC ZITG NVGA PDNS LGGP CWPU XSCP TUOO NHQC

• Bold letters get tallied

• The computer does this with modulo **if** (index **mod** key_len) == curr_key_pos

Frequencies



- Computer takes the Dot Product of the Peaks of the graph to determine the key letter.
- After Iterating through all the positions in the keyword, the final keyword is decided.



Sources

Simmons, Gustavus J.. "Vigenère cipher". Encyclopedia Britannica, 14 Jul. 2021, <u>https://www.britannica.com/topic/Vigenere-cipher. Accessed 22 April 2022</u>.